

# Peak Wave Period and Direction Estimation Using 3D FFT on Monoscopic Videos

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# Context: SeaLab, a semi autonomous sailboat

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## Why an "intelligent" sailboat?

- Wind powered: no carbon emissions
- Helping the crew make decisions



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- Helping the crew make decisions

## Giving SeaLab "intelligence"

- regular marine sensors: anemometer, compass, GNSS...
- **Single consumer camera** fixed on mast, filming the sea surface at an oblique angle
- multiple inertial sensor units, computing power, blackbox capabilities...
- Should stay cheap and low power



## Estimating the sea state onboard

- Sea state affects vessel performance, safety and routing
- Sea state: agitation of the sea
- Key parameters: significant wave height  $H_s$ , peak frequency  $f_p$ , direction  $\theta_p$

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- Wave buoys: costly, not onboard
- Radar systems: energy-intensive
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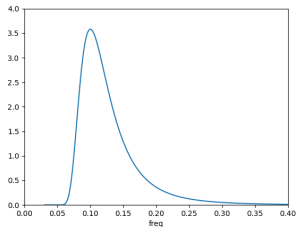
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## Our goal

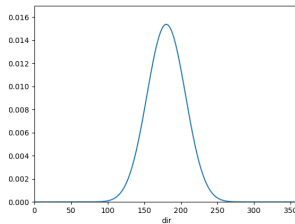
Estimate wave parameters from a **single onboard video camera**.

# Ocean Wave Modeling: Wave spectrum

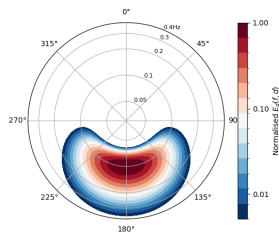
The wave field is described by the **directional spectrum**  $S(f, \theta)$ .



$S(f)$

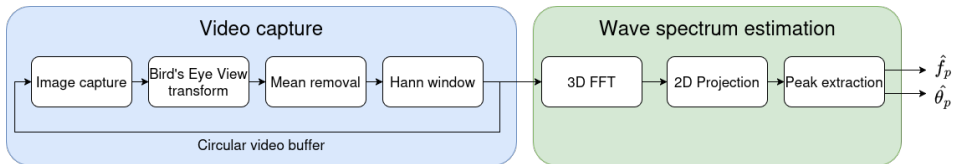


$G(\theta)$



$S(f, \theta)$ :  $f_p = 0.1$  Hz,  $\theta_p = 180^\circ$

# Method Overview



1. **Video stabilization** (not required for static cameras)
2. **Bird's Eye View (BEV) transform** to remove perspective distortion
3. **Preprocessing**: DC removal + 3D Hann windowing
4. **3D FFT**: spectral analysis over  $(x, y, t)$
5. **Wave spectrum extraction**: convert to  $S(f, \theta)$
6. **Peak extraction**: estimate  $\hat{f}_p$  and  $\hat{\theta}_p$

## Step 2: Bird's Eye View Transform

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**Goal:** suppress perspective effects so that wave frequencies are uniform across the image.

Uses the **pinhole camera model**:

$$u = KMX_w = PX_w$$

Inverse mapping onto the  $z = 0$  plane:

$$X_w = (PL)^{-1}u$$

Homography  $H = P_2L(P_1L)^{-1}$  maps pixels from camera view to top-down view.



Original frame



After BEV transform

## Step 3 & 4: Preprocessing and 3D FFT

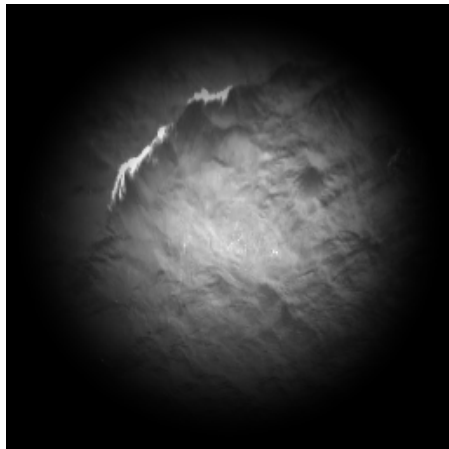
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### Preprocessing of the video cube $z(x, y, t)$ :

- **DC removal:** subtract mean pixel value across frames to enhance low-frequency precision
- **3D Hann window:** reduce spectral leakage, sharpen frequency peaks

### 3D Discrete Fourier Transform:

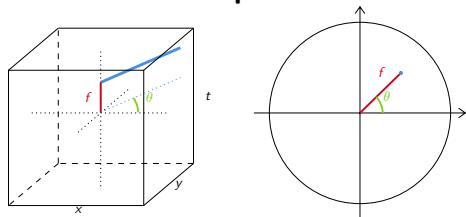
$$\mathcal{Z}(k_x, k_y, \omega) = \sum_x \sum_y \sum_t z(x, y, t) e^{-i(k_x x + k_y y + \omega t)}$$



After DC removal and windowing

## Steps 5 & 6: Spectrum Extraction and Peak Detection

From 3D Fourier space to directional spectrum:

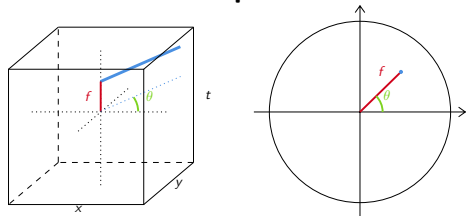


$$\sum_{i=0}^{N/2} a\left(\lfloor i \sin \theta \rfloor + \frac{N_x}{2}, \lfloor i \cos \theta \rfloor + \frac{N_y}{2}, f + \frac{N_t}{2}\right)$$

Cylindrical projection of the 3D amplitude cube. Wave-length information is traded for a compact  $(f, \theta)$  representation.

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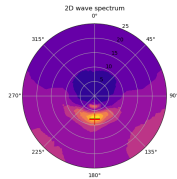
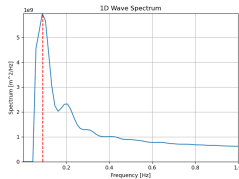


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Peak extraction:

- Peak frequency:  $\hat{f}_p = \arg \max_f S(f)$ ,  
where  $S(f) = \int S(f, \theta) d\theta$
- Peak period:  $\hat{T}_p = 1/\hat{f}_p$
- Peak direction:  $\hat{\theta}_p = \arg \max_{\theta} S(\hat{f}_p, \theta)$



1D and 2D estimated spectra

# Evaluation: Synthetic Dataset

Blender simulations with Tessendorf ocean algorithm and JONSWAP spectrum.

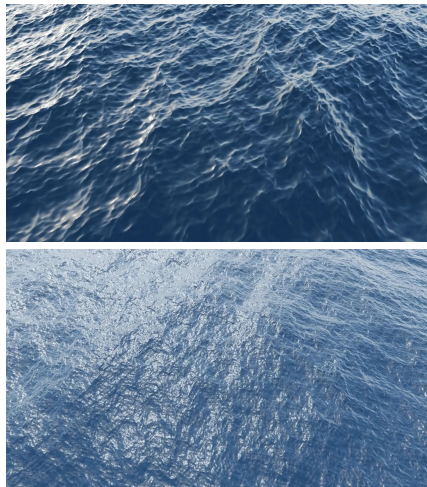
- 684 sequences total (171 per sea state)
- 600 frames at 30 fps (20s each)
- Random peak direction  $\theta_p \in [0^\circ, 360^\circ]$
- Random sun position: varying lighting

| Sea state | $f_p$ range  | $H_s$ range |
|-----------|--------------|-------------|
| 3         | 0.16-0.18 Hz | 0.65-0.80 m |
| 4         | 0.11-0.13 Hz | 1.35-1.65 m |
| 5         | 0.09-0.10 Hz | 2.25-2.75 m |
| 6         | 0.07-0.08 Hz | 3.50-4.50 m |



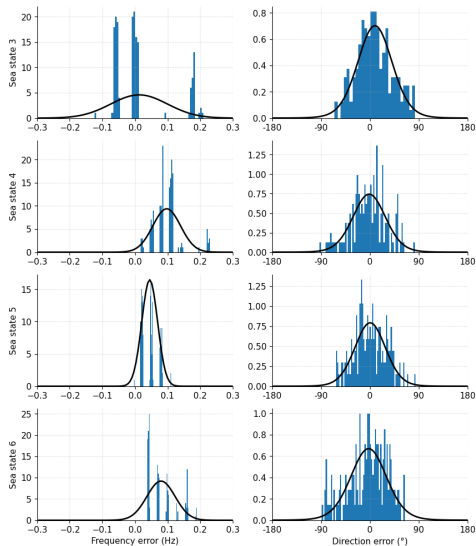
Dataset publicly available:

<https://l3i-share.univ-lr.fr/2026OceanSimulationDataset>



Simulation examples

# Results: Synthetic Data



Error distributions by sea state

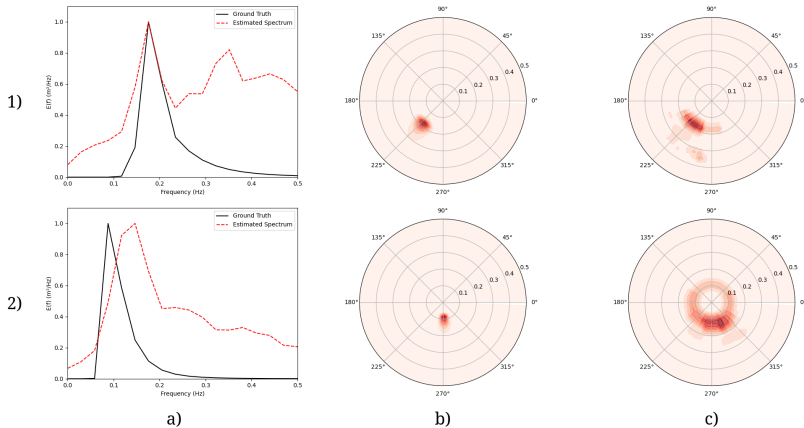
## Direction estimation:

- Mean error  $\approx 0^\circ$
- Std. deviation  $\approx 30^\circ$

## Frequency estimation:

- Bias  $\approx 0.05$  Hz
- Std. deviation  $\approx 0.06$  Hz

# Results: Synthetic Spectra Examples



Row 1: sea state 3, minimal estimation errors.

Row 2: sea state 5, maximal objective errors, yet visually plausible.

(a) 1D spectrum with ground truth (black) and estimate (red); (b) GT directional spectrum; (c) estimated directional spectrum.

# Evaluation Real Dataset (Black Sea 2011)

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**Dataset:** Guimarães et al. (2020) stereo-vision sequences with wave gauge reference (5-sensor star array).

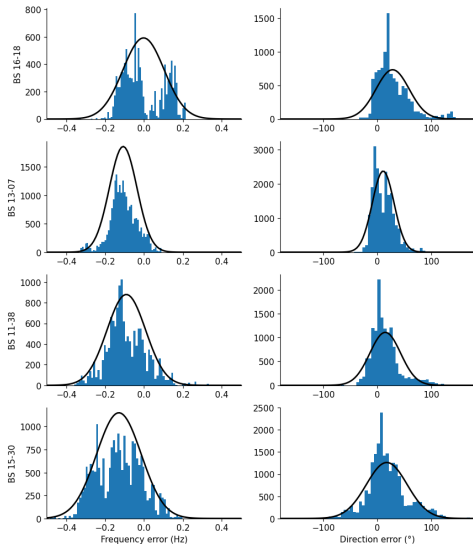
| Time  | fps | $f_p$   | $\theta_p$ |
|-------|-----|---------|------------|
| 16:18 | 15  | 0.33 Hz | WSW        |
| 11:38 | 12  | 0.38 Hz | WSW        |
| 13:07 | 12  | 0.33 Hz | SW         |
| 15:30 | 12  | 0.27 Hz | SW         |

~68 000 images, calm sea state ( $H_s = 0.30\text{-}0.55$  m).



Example frame from real sequence

# Results: Real Data



Error distributions, Black Sea sequences

## Direction:

- Bias  $\approx 15^\circ$  toward South
- Std. deviation  $\approx 20^\circ$

## Frequency:

- Bias  $\approx -0.1$  Hz
- Std.  $\approx 0.1$  Hz
- Sequence 16:18 shows bimodal error: wind sea + swell

# Computational Complexity

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**Dominant cost:** 3D FFT

$$\mathcal{O}(N^3 \log N), \quad N = N_x \cdot N_y \cdot N_t$$

**Experimental setup:**

- Intel Core i9-12900H, 32 GiB RAM
- 1024 images at  $256 \times 256$  px
- $N = 256 \times 256 \times 1024 = 2^{26}$

## Per-iteration cost

**2.9 s** wall-clock time

**2.4 GiB** memory

# Conclusion & Future Work

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## Summary

- 3D FFT on stabilised BEV video estimates  $\hat{f}_p$  and  $\hat{\theta}_p$
- Validated on synthetic and real dataset
- Direction: consistent accuracy
- Frequency: sufficient precision but systematic bias
- Runs in  $\approx 3$  s per window. Compatible with near-real-time use

## Future work

- Fusion with onboard sensors: IMU, wind sensor, water speed
- FPGA deployment for real-time embedded processing
- **Real-world dataset** from a camera on a sailing boat mast

Thank you!